



Understanding teachers' practices and professional geneses with technology

Mariam Haspekian

► To cite this version:

Mariam Haspekian. Understanding teachers' practices and professional geneses with technology. International Congress on Mathematical Education, ICME 2012, Jul 2012, Seoul, South Korea. hal-01273878

HAL Id: hal-01273878

<https://hal.science/hal-01273878>

Submitted on 14 Feb 2016

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

UNDERSTANDING TEACHERS PRACTICES AND PROFESSIONAL GENESES WITH TECHNOLOGY

Mariam Haspekian

EDA, University of Paris Descartes, France

mariam.haspekian@parisdescartes.fr

Abstract: This paper shares some research reports and presents some results concerning teachers' professional genesis with spreadsheets by bringing closer the results obtained in different research. It aims at gaining insight into the teachers practices with technology and how these practices evolve in time. Comparing the evolution of an ordinary teacher integrating spreadsheet in her practices with the practices of teachers expert with spreadsheet, we find some similarities in the way of using this too, and make some hypotheses on the importance of these common elements as key issues in ICT integration.

Keywords: ICT, spreadsheet, instrumental (professional/ personnal) geneses, instrumental distance.

INTRODUCTION AND THEORETICAL NOTIONS

How does technology influence mathematics teaching and learning? 25 years after the first ICMI study on this theme (Cornu & Ralston, 1992), the second one was revisiting the subject and, as Michèle Artigue notes it (2008), if our knowledge certainly increased, the situation did not much evolve. Many reports deplore the poor integration of ICT in mathematics teaching and researchers stress a phenomenon of “disappointment” after an enthusiastic period where pioneers claimed ICT benefits for learning. One of the reasons advanced is the “teacher barrier” (for instance Ruthven 2007 or Balanskat, Blamire & Kefala 2006), specially the importance of teachers' practices, seen as a key issue. This is why it seems crucial to advance in the comprehension of practices and instrumental geneses with ICT.

To contribute to this issue, in this paper, we put in perspective the data we collected in various researches (Haspekian 2005, 2008, 2011) that were adresssing various teacher profiles: experts with ICT, preservice teachers and teacher not novice but not expert of the ICT.

To analyse these data, we have used in our thesis (2005) two theoretical frameworks: the instrumental approach (Artigue 2002, Guin, Ruthven & Trouche 2004) developed around the concept of instrumental genesis, and the didactic and ergonomic aproach (Robert & Rogalski, 2002) which describes teacher's activity through 5 components: personal, mediative, cognitive, but also institutional and social one. Since then, applying these theories, we have the material now to stress some results about the genesis of ICT use in teachers' practices, the way they develop, the difficulties encountered and the comprehension of how technology integrates these practices. Thus, they are also interesting for teachers' training perspectives.

In the following, we present first the theoretical notions used to analyse our data.

Theoretical notions

(a) Didactic and ergonomic approach (Robert and Rogalski, 2002)

Concerning the integration of calculators, Trouche (1999, p. 307), in a research led on the initial training of teachers, had already noticed the importance of two factors relative to the teachers: their degree of mastering the tool and the conception (more or less negative) which they had of this very integration. In the same way, the numerous works analyzing practices underlines that teachers activity does not necessarily follow only contents reasons (about mathematical knowledge) or learning reasons (on students's side) but also arguments on the teachers'side seen as individuals exercising a job with its own constraints and liberties. According to the didactic and ergonomic approach (Robert and Rogalski, 2002), the *cognitive* and *mediative* components relate to the choices made by the teacher in the spatial, temporal and mathematical organisation of the lessons. These choices are made according teachers' *personnal* component. But teachers are not totally free in these choices. They are more or less constrained by *institutional* and *social* dimensions. The personal component relates to the teacher as a singular subject, with his own history, practices, vision of mathematics learning... The institutional and social dimensions relate to curricula, lessons duration, school social habits, mathematics teachers habits etc. In the case of ICT practices, instrumental aspects seem to interfere with each of these components, particularly, the personnal one plays of course a crucial role in the integration or not of ICT in mathematics. This lead us to use the instrumental approach quoted above, in order to analyse more locally some of the phenomena observed with ICT practices, and particularly two notions that the results rely on: the idea of instrumental distance and the teachers' professionnal intrumental genesis with the tool.¹

(b) Instrumental Distance

In French curricula, dynamic geometry software are prescribed as much as spreadsheets. But the previous find a better integration in mathematics classroom than the second. In our thesis we found that the notion of *distance* to the referential environment plays an imporant role in the explanation of this phenomenon.

We have introduced the idea of *distance* to take into account, beyond the “computer transposition” (Balacheff, 94), the set of changes (as cultural, epistemological or institutional) introduced by the use of a specific tool in mathematics “praxis”. For a given tool, a too big distance to the “current school habits” is a constraint on its integration (Haspekian, 2005b). On the other hand, didactical potentialities of technology rely on the distance it introduces as regard to paper-pencil (as for instance providing new representations, new problems, increasing calculation possibilities...). In our thesis (Haspekian 2005a) we have brought out 4 types of elements that can generate some distance. Some are directly linked to the *computer transposition*: as the representations and the associated symbolism. But some can also be of an *institutional nature*², or still *didactical nature* (vocabulary, field of problems they allow to

¹ Note that this idea is different from the idea of “genese d'usage professionnel” also developed in French research

² Beyond the computer transposition that modifies the mathematical objects, the modification, from an institutional point of view, concerns actually the whole ecology of these objects (tasks, techniques, theories can be modified). The idea of “distance” reflects this gap between the praxeologies associated to two different environment (considering paper pencil as a peculiar environment of the mathematical work)

solve...), or at least *epistemological* one (what gives tool an epistemological legitimacy). This is linked to teacher's personal component (her representations of mathematics, of mathematics teaching, of the role this tool plays in the development of mathematics).

(c) Professional instrumental genesis

Then, the way teachers orchestrate and support pupils' instrumental geneses evolves year after year. Considering spreadsheet as an instrument for the teacher, allowing her to achieve some teaching goals, we consider a process of instrumental genesis *on teacher's side* (Haspekian, 2006). The same artefact, the spreadsheet, becomes an instrument for pupils' mathematical activity and an (other) instrument for teacher's didactical activity. Thus, applying the instrumental approach to the spreadsheet seen as a *teaching* instrument built by the teacher along a professional genesis, we can bring out two processes:

An instrumentalization process: the tool is instrumentalized by teacher in order to serve her didactic objectives. It is distorted from its initial functions and its didactical potentialities are progressively created (or "discovered" and appropriated in the case of an educational tool).

An instrumentation process: teacher, as a subject, will have to incorporate in her teaching schemes that were relatively stable some new ones integrating the tool use. Teacher will progressively specify the tool use to a particular class of situations (as "take advantage of spreadsheet for algebra learning") and organise her activity in a way progressively invariant for this class of situation (Dan's case already shows some regularities from year 1 to year 2).

Bringing together the results from different researches

In the following of this paper, we are bringing together the results of two different research. The first one concerns the practices of what we have called "experts" teachers, they are teachers who integrate ICT for a long time and are besides "ICT trainers" in mathematics teacher training. By comparing their practices between them and also with the practices of preservice teachers, we have highlighted some characteristics of the practices with ICT.

The second research is a two years case study of a teacher, named Dan in the following. She is a long experienced teacher but integrating the spreadsheet for the first time in her practices. The case of the spreadsheet is a good revealing of the phenomena that come into play in the development of practices integrating ICT for at least two reasons. First, the spreadsheet is a professional tool without any didactical functionality given a priori. The instrumental distance in this case is not negligible and plays a considerable role in the difficulties of the spreadsheet integration. Second, the teacher has to turn this non educational tool into a didactical instrument through a professional genesis, which is here again rather complex, partly because of this instrumental distance. The study observed the way Dan integrates spreadsheet in her practices and the evolution of this integration over her first two years.

What is interesting then to notice, when bringing together these research, is that Dan evolves with the spreadsheet towards the characteristics of experts' practices. The §.2 aims at showing some of the results obtained with experts teachers, the §.3 describes Dan's case study and evolution which, by reducing the distance, goes towards expert practices.

FIRST RESEARCH : SOME CHARACTERISTICS OF EXPERTS PRACTICES WITH ICT

Are there regularities in the practices among the teachers who successfully integrated the spreadsheet? We looked for regularities at the following levels: in teachers conceptions, in the evolution of their practices and in the changes this evolution led to. These questions can be first enlightened by the notions of "coherence" and "stability" as Robert & Rogalski quoted it:

"the coherence of the system of the practices of a teacher (...) would prevent the introduction of inconsistent elements with this system" (Robert & Rogalski, 2002, p. 521).

Similarly, but with another theoretical framework, Lagrange (2000) underlines that the introduction of a tool in mathematics lessons generates an upheaval of the praxéologies which is a factor of non integration of the tool. How do experts deal with these obstacles? We carried out questionnaires and interviews with trainees and "experts" (teachers who are integrating spreadsheet in their class and are teacher-educators on ICT). In the case of trainees, we had group discussions so that teachers exchange, discuss, which emphasizes their opinions. With the experts we had individual interviews with an additional part concerning their practices.

We present below two results obtained with the experts, in comparison with the results obtained with the beginners. We stress some common lines among the **novices** (as their obvious difficulties to perceive the **potentialities of the tool**, to conceive organizations which they have never seen), and some convergences among experts practices that can be connected to their success to integrate spreadsheets.

The first result concerns the tasks given with spreadsheet. A common part of the questionnaires addressed to experts and novices was constituted by a set of tasks, from a basic use of the spreadsheet, as a mere calculator, to a more interesting use of the spreadsheet potentialities (based on research situations mentioned in Capponi 2000, Arzarello & al. 2001, or Rojano & Sutherland 1997, and analysed by their authors as being positive for mathematics learning). Thus, we were presenting different way of using spreadsheet and teachers had to choose which of these situations were interesting for **mathematics** teaching and learning.

The results join those mentioned already in research (Laborde 2001, Monaghan, 2004) : novices, nonexpert of spreadsheet, hardly identify tool's potentialities and interesting situations. The choices of the beginners, and their arguments, were systematically opposed to those of the experts (which corresponded to the interesting situations). Teachers first approach of spreadsheet use is not the best way of benefitting from technology potentialities. As Artigue recalls it, the observed (and quite understandable) tendency consists in using technological tools not for their epistemic value (helpful mean of understanding mathematical objects) but just for their pragmatic value (produce results quickly and easily) in some tasks very similar of those traditionally given in paper-pencil environment (Artigue, 2002).

The second result concerns some common characteristics in experts' practices as the importance of taking into account not a single tool but a system of instruments. Two characteristics appear to contribute fundamentally to their success in integrating spreadsheets: **a game "ancient / new "** playing both at the level of the mathematical contents and at the level of the instruments, and a certain **art/skill** to know how to mix these levers.

These characteristics provide an economic functioning both on the management of the class in ICT sessions, and on the management of pupils' instrumental geneses. For example, at the level of the contents, one expert says having “*a way of making revisions by bringing something more*”. Another says he has “*the same notions presented in two different environments*”. For another one, she systematically works again by hand after ICT session and combines paper-calculator-spreadsheet: “*I make links non-stop, again and again...*”

For all of them, it is this orchestration of a whole system of instruments that becomes a base to support spreadsheet integration: this tool being perceived as more complex, they make their pupils meet it after other software. This allows **a gain of time** on the management of class in ICT session (discover the class, organize the contract, etc.) and **a gain of time** on the instrumental geneses with spreadsheet, a part of it being taken through other tools (physical manipulation of the material, the computer, virtual manipulation of files,...).

In the common characteristics, we also found an increased attention paid to the questions of “mutualisation” and “socialisation”. Two elements are used for that: first, the experts are all organising their sessions with pupils working in pairs, second, they have the habit to use the videoprojector in order to mutualise here again the scattered knowledge and make the contents more homogeneous (mathematical knowledge but also instrumental knowledge).

SECOND RESEARCH: A TWO YEARS CASE STUDY

Dan is not a trainee³, but she is not an expert with ICT in mathematics teaching. She has experienced dynamic geometry software and integrates now spreadsheet for the first time. We collected data that very first year and the year after. The observations show some evolutions from a year to the next one. As we said, we will see that this evolution with the spreadsheet converges towards the characteristics of experts' practices described above.

During the first year, Dan was motivated by her participation in a research project focusing on spreadsheet use for *algebra* learning (Haspekian 2005a). At the end of the research, an interview collected her thoughts and feelings about this experience. The following year, she uses the spreadsheet by her own choice, without any research protocol. On that occasion, we recorded her first spreadsheet session and the following session in a paper and pencil environment. Some phenomena during this observation and the way Dan evolved in her practice with spreadsheet as a didactical tool provide interesting data. Let us first present the evolutions at stake and then describe the theoretical frames to analyse these data.

During the second year, Dan introduced spreadsheet not with algebra but with statistics (headcounts, frequencies and cumulative frequencies after having seen these notions in paper pencil environment). In this context, some of the observed elements are surprising: the lesson shows very little statistics, is mostly centred on the tool functionalities, and reveals unexpected mathematics (notions of variable, formula, distinction “numeric/algebraic” function...). These latter reflect the influence of year 1 experience, centred on algebra, but this does not explain all the evolution year 2 (variations and regularities) summarized in Table 1:

³ she's been teaching for more than 10 years

| Use of spreadsheet | Year 1 | Year 2 |
|--|---|---|
| VARIATIONS | | |
| Class level | 7 th Grade (12 year old) | 8 th Grade (13 year old) |
| Old/new content | New | Old |
| Mathematical Domain | Algebra | Statistics |
| Spreadsheet location | Limited to computer lab | Computer lab +ordinary classroom |
| Synthesis | No | Yes |
| Interactions Teacher-Students | Mostly individual | Individual and collective |
| Use of the video and collective presentation | Piloted by teacher, limited role | Teacher and student. Important role |
| Students Configuration | Work by pairs | Work by pairs + collective work: one student at the board |
| REGULARITES | | |
| Maths objectives, teacher aims | Algebra | |
| Additional material | Worksheet for pupils and pre-organised spreadsheet file | |
| Institutionalisation | In an ulterior lesson, in ordinary classroom | |

Table 1. Comparison Year 1- Year 2

Table 1 shows an evolution of 3 components: the mediative and cognitive components (mathematical domain chosen, way of introducing spreadsheet, class level, etc.) have evolved along the two years. This indicates (and is confirmed by the phenomena observed during the lesson) that the personal component of Dan evolved too. What can we say about this evolution and why?

How to understand Dan's evolutions?

Spreadsheet is not given as didactical tool to serve mathematics education. It may progressively become such an instrument along a professional genesis. Thus, the way teachers orchestrate and support pupils' instrumental geneses evolves year after year. The way Dan evolved from a year to another concerns this professional instrumental genesis.

For instance, using both the notions of distance and double instrumental genesis in Haspekian (2008), we have described and analyse the beginning of such a genesis and the complexity that comes along with through the case of Dan's use of spreadsheet: Dan builds up some *schemes of instrumented action*⁴ with the goal of using spreadsheet to teach algebraic concepts (variables, formulae, for instance through the use of the recopy, or by taking benefits of the numerical feedback to infer the equivalence of two formulae etc.). This brings into play some usage schemes concerning material aspects as: the tool integration in a larger set of instruments (with the video projector), the organisation of the lessons, schemes that undertake the orchestrations. Some of the different elements that are part of her orchestrations have been modified next year by including the following regular elements: (a) using a video projector at the beginning of the session to make collective explanations, (b) making pupils communicate and work by pairs, (c) giving pupils a sheet of instructions and a pre-built computer file to

⁴ Rabardel (2002) distinguishes two types of schemes: *usage schemes* (related to the *material* dimension of the tool) and the *schemes of instrumented action* (related to the global achievement of the task, with goals and intentions).

gain time, (d) regularly “click” on cell to check whether pupil have edited a formula or numerical operation, or even directly the numerical result...

These elements are part of Dan’s instrumental schemes which are moving along with the following evolutions that we have observed: **(a) Higher level of class** : she uses spreadsheet with 8th graders instead of 7th graders, **(b) Lower quantity of « new » concepts**: not mix the introduction of the spreadsheet with the introduction of new mathematical notions, **(c) Domain change**: introduce the tool with statistics which seemed to Dan more appropriate than algebra, **(d) Deeper articulation between social and individual schemes**, the importance of the articulation in instrumental geneses has been mentioned by Trouche, (2005) (in the interview, Dan says she did not organise moments of mutualisation enough and she explicitly wished to take care of this point the 2nd year).

Observing deeper these evolutions, they all appear to converge in the direction of *reducing* the instrumental distance. Indeed, as we will see, at different levels, Dan’s modifications year 2 tend to decrease the spreadsheet’s too big instrumental distance:

(d) Changing the class level: Higher level of class

This modification comes with the change of the domain (c): in French curricula, spreadsheet is explicitly mentioned with statistics for 8th Grade pupils, whereas it. In appears in a more general and vague way for 7th Grade curriculum, requiring from teachers a deeper work to define its potentialities for learning mathematics. These latter appear more distant from spreadsheet mathematics than in the 8th Grade, where spreadsheet appears clearly in relation with precise notions. Thus, choosing this level allows Dan to reduce the distance and match more easily with the official prescriptions. Besides, year 1, Dan found pupils’ instrumentalisation not easy in 7th Grade (difficulty to use the “recopy”, to select a single cell, to edit a formula). Older pupils seem to be more skilful and problems linked to instrumentalisation should be less interfering with the mathematical work. With 7 Graders, manipulations of the tool seemed more difficult and the tool appeared less transparent.

(e) The “old/new” game in the mathematical and in the instrumental contents

Year 1, Dan introduced both a new tool and new mathematical contents (algebraic notions). The ratio old/new is different in year 2 and also goes towards reducing the distance by reducing the part of “new”: all the mathematical notions at stake in the spreadsheet session (headcounts, frequency, cumulative frequency) had previously been seen in paper pencil environment. This work (new environment with “already-seen” concepts) will then serve Dan as a base to work algebraic notions (new concepts in an “already-seen” instrument).

(f) Domain changing

The mathematical domain chosen by Dan year 2 also reduces the distance for at least three reasons. Statistics are usually seen to be more in conformity with spreadsheet work than algebra. Furthermore institutional pressure is less important in statistics than algebra, a more classic and traditional domain strongly linked to paper pencil mathematics. On the contrary, statistics are nowadays seen as more fitted to technologies. At last, in the spreadsheet language, one can find more common terms with statistics whereas the distance to the traditional algebraic vocabulary is important (Haspekian 2005b).

(g) Moments of mutualisation and articulation with paper-pencil mathematics

Dan introduced year 2 some moments of mutualisation in spreadsheet sessions. In the interview, she affirmed her will to increase the similarity with the traditional sessions. She said having the feeling that it is necessary to multiply the links with the paper pencil mathematics (for instance, she started the sequence by a paper- pencil session, then worked the same notions in a spreadsheet session, then she came back on the work done with spreadsheet in a paper pencil session, etc.).

Reducing distance... Towards experts' practices

All these actions contribute to reduce the distance with paper-pencil, to mix these two environments in a greater proximity. But if we go back now to the results obtained in the research with expert teachers, Dan's evolution tends to join experts practices.

Indeed, we have seen that in their practices, this "mixing" of different environment appeared as a key point to integrate spreadsheet. Teachers who used to integrate spreadsheet had precisely these characteristics. It is thus interesting to notice that Dan's professional genesis follows the same line. For instance, the moments of mutualisation and articulation with paper-pencil mathematics are better thought the second year by Dan, whereas she did not pay much attention on it the first year. This has been seen as we mentioned it in §.2 as an important characteristics of expert teachers.

The "old/new" game mentioned above is another characteristic found in the expert practices. They manage ICT integration by adjusting and adaptating the degree of novelty to to degree of complexity of the tool: to introduce a complex artefact such as the spreadsheet, they choose ancient contents (already seen in paper pencil environment), once spreadsheet is seen on ancient contents, they can use it next time to introduce new mathematical knowledge.

We can note that here again Dan's evolution goes in that direction. First year she introduce both spreadsheet and a new mathematical domain (algebra), whereas the year 2, she chooses for that a domain (statistics) previously studied in paper-pencil; pupils meet the new instrument on an old content. Dan's long term intention, as she said in the interview, is to use spreadsheet to work algebra, but now she will do it after pupils having seen the spreadsheet on another content (an old one) in order not to intruduce both new artefact and new contents.

Of course, the year 2, Dan had not all the characteristics of the experts as evoked in §.2, but this is not surprising. She is at a stage on her professional genesis with the spreadsheet, integrating it for the second time. It is predictable that this stage is not yet stabilized and that she is evolving. For instance, for the experts, the game old/new concerns also the instruments, not only the mathematical contents. We have seen in §.2 that experts make pupils meet computers with *another* software than spreadsheet, such as dynamic geometry, which present a lesser distance than the spreadsheet. In that way, pupils meet ICT classroom, instructions about the use of computers, files, opening and closing sessions, articulation with paper-pencil, work in pair and so on, within a software that seems easier to integrate. Once they are used to these bases and orchestrations on an old instrument, they are ready to meet a new one, less easy, such as the spsreadsheet. In Dan's evolution, we do not see yet this exploitation of different instruments to facilitate spreadsheet introduction, but it seems

reasonable to think that one does not gain all the experts' characteristics in one year practice. This instrumental professional genesis is a long process, as for any instrumental genesis.

CONCLUSION AND PERSPECTIVES

As we saw, we can explain Dan's evolutions in terms of a *reduction* of the distance (either by making this distance more explicit or by alternating work in the environments enriching both of them). Integrating spreadsheet constitutes a significant creative task for teachers as the tool is not given with any didactical functionalities. It requires a professional instrumental genesis on teacher's side different from the personal genesis with the tool (even if they interfere, see Haspekian 2011) and also different from that on pupils' side.

These combined considerations helped us to analyse Dan evolution and to note that in her evolution she tends to acquire some of the characteristics found as a common line among expert teachers: Articulation with paper-pencil mathematics, Moments of mutualisation and socialisation, an the Game ancient/new, playing on the contents (not yet on the instruments).

We suggested that these elements are key issues in ICT integration but we need a larger panel. Our first research with experts concerns 6 teachers. The fact that Dan's evolution tends towards some of their common characteristics is an indication that these elements may constitute good "candidates" of ICT practices, but this needs research at a larger scale.

Finally, several questions remain. Understanding better characteristics of experts' practices and of course the way to acquire them for teacher, are important in a training perspective and still open research fields. We also made the hypothesis that in the questions of ICT integration but also in these questions of practices evolutions, a criteria which seems important is this notion of instrumental distance. If it is a source of difficulty for teachers, it is also necessary to determine which elements may counterbalance the distance and play in favor of the tool integration, such as institutional injunctions, or tool's epistemic value, didactical design...

References

- Artigue, M. (2008). L'influence des logiciels sur l'enseignement des mathématiques : contenus et pratiques, *Actes du séminaire DGESCO de février 2007*, http://eduscol.education.fr/D0217/actes_math_et_tice.pdf
- Artigue, M. (2002). Learning mathematics in a CAS environment: The genesis of a reflection about instrumentation and the dialectics between technical and conceptual work. *International Journal of Computers for Mathematical Learning*, 7, 245-274.
- Arzarello, F., Bazzini, L., Chiappini, G. (2001) A model for analysing algebraic processes of thinking. In R. Sutherland, T. Assude, A. Bell and R. Lins (dir.), *Perspectives on school algebra*, vol.22, pp. 61-81, Kluwer Academic Publishers.
- Balacheff, N. (1994). La transposition informatique. Note sur un nouveau problème pour la didactique. In M. Artigue (Ed.), *Vingt ans de Didactique des Mathématiques en France*, pp. 364-370. Grenoble : La pensée sauvage.
- Balanskat, B., Blamire, R., Kefala, S. (2006). The ICT Impact Report. A review of studies of ICT impact on schools in Europe. *Report by European Schoolnet in the framework of the European Commission's ICT cluster*. http://ec.europa.eu/education/pdf/doc254_en.pdf

- Capponi B. (2000) Tableur, arithmétique et algèbre. L'algèbre au lycée et au collège, *Actes des journées de formation de formateurs 1999*, p.58-66, IREM de Montpellier.
- Cornu B, & Ralston A. (eds) (1992). *The influence of computers and informatics on mathematics and its teaching*. Science and Technology Education. 44. Paris : UNESCO.
- Drijvers, P., Kieran, C., Mariotti, M.A. (2010). Integrating technology into mathematics education: theoretical perspectives. In C. Hoyles & J.-B. Lagrange (Eds.), *Mathematics education and technology-Rethinking the terrain* (pp. 89-132). New York: Springer.
- Guin, D., Ruthven, K. Trouche, L. (Eds.). (2004). *The didactical challenge of symbolic calculators*. New York: Springer.
- Haspekian, M. (2011). The co-construction of a mathematical and a didactical instrument. Proceedings of the Seventh Congress of the European Society for Research in Mathematics Education (CERME 7), Rzeszow, Poland, February, 9– February, 13, 2011. http://www.cerme7.univ.rzeszow.pl/WG/15a/CERME7-WG15A-Paper23_Haspekian.pdf
- Haspekian, M. (2006). Evolution des usages du tableur. In Rapport intermédiaire de l'ACI-EF Genèses d'usages professionnels des technologies chez les enseignants, <http://gupten.free.fr/ftp/GUPTEn-RapportIntermediaire.pdf>
- Haspekian, M. (2005a). Intégration d'outils informatiques dans l'enseignement des mathématiques, Etude du cas des tableurs. (Doctoral dissertation, University Paris 7, France) Available from. tel.archives-ouvertes.fr/tel-00011388/en/
- Haspekian, M. (2005b). An “Instrumental Approach” to study the integration of a computer tool into mathematics teaching: The case of spreadsheets, *International Journal of Computers for Mathematical Learning*, 10, 109–141.
- Laborde, C. (2001). Integration of technology in the design of geometry tasks with Cabri. *International Journal of Computers for Mathematical Learning*, 6/3, 283-317
- Lagrange, JB. (2000). L'intégration d'instruments informatiques dans l'enseignement : une approche par les techniques, *Educational Studies in Mathematics*, 43, 1-30
- Monaghan J. (2004) Teacher's activities in technology-based mathematics lessons. *International Journal of Computers for Mathematics Learning*. Vol 9, 327-357.
- Robert, A.& Rogalski, J. (2002). Le système complexe et cohérent des pratiques des enseignants de mathématiques : une double approche, *Revue canadienne de l'enseignement des sciences, des mathématiques et des technologies*, 2, 505-528.
- Rabardel, P. (2002). *People and technology -a cognitive approach to contemporary instruments*; <http://ergoserv.psy.univ-paris8.fr>
- Rojano T., Sutherland R. (1997) Pupils' strategies and the Cartesian method for solving problems: the role of spreadsheets, *Proceedings of PME 21*, vol. 4, p. 72-79.
- Ruthven, K. (2007). Teachers, technologies and the structures of schooling. In D. Pitta-Pantazi, & G. Philippou (Eds.), *Proceedings of CERME 5*, pp.52-68, Larnaca.
- Trouche, L. (2005). Instrumental genesis, individual and social aspects. In D.Guin, K. Ruthven & L. Trouche (Eds.), *The didactical challenge of symbolic calculators: turning a computational device into a mathematical instrument* (pp.197-230). New York: Springer